MODELING OF OVERHEAD TRANSMISSION LINES FOR LIGHTNING OVERVOLTAGE CALCULATIONS

MODELACIÓN DE LÍNEAS AÉREAS DE TRANSMISIÓN PARA EL CÁLCULO DE SOBRETENSIONES ORIGINADAS POR EL RAYO

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RESUMEN

Un modelo de línea aérea de transmisión adecuado para el cálculo de sobretensiones originadas por el rayo debe incluir varias partes de la línea: conductores de fase y cables de guarda, torres, puestas a tierra, cadenas de aisladores y distancias en el aire. Un componente adicional, el pararrayos, puede ser necesario si el estudio tiene como objetivo evaluar el comportamiento frente al rayo de una línea de transmisión protegida mediante pararrayos. Este último aspecto es importante ya que el modelo a utilizar puede variar según se hayan instalado o no pararrayos para proteger la línea. El rayo es un fenómeno físico de naturaleza aleatoria. El cálculo de la tasa de contorneos (flameos) causados por descargas atmosféricas ha de realizarse teniendo en cuenta este aspecto, así como el comportamiento aleatorio que pueden tener algunos componentes de la línea aérea; por el ejemplo, las cadenas de aisladores. El objetivo de este artículo es doble: por un lado, se analizan las directrices propuestas hasta la fecha para representar líneas aéreas de transmisión en el estudio de sobretensiones atmosféricas y, por otro, se propone una metodología para seleccionar el modelo más adecuado de línea aérea de transmisión cuando se utilice una herramienta de simulación en el dominio del tiempo; por ejemplo, un programa tipo EMTP. Esta metodología es aplicada a un caso concreto de línea aérea de transmisión.

Palabras clave: Sobretensiones, rayos, modelación, simulación, líneas aéreas de transmisión, aisladores, pararrayos, puesta a tierra, análisis paramétrico, EMTP.

ABSTRACT

Several parts of an overhead transmission line have to be included in a model adequate for lightning overvoltage studies: wires (shield wires and phase conductors), towers, grounding, insulator strings and air clearances. An additional component, the surge arrester, should be added if the study is aimed at determining the lightning performance of a transmission line protected by surge arresters. This latter aspect is important since it can affect the model to be used for representing some parts of the line. Lightning is a physical phenomenon of random nature. The calculation of the lightning flashover rate must be performed taking into account this aspect, as well as the random behavior of some line component; e.g., insulator strings. The aim of this paper is twofold: on one hand, it presents a discussion about modeling guidelines proposed to date for representing overhead transmission lines in lightning studies; on the other hand, it proposes a methodology for selecting the most adequate model of an overhead transmission line in lightning overvoltage calculations, when using a time-domain simulation tool, e.g. an EMTP-like tool. This methodology is applied to a test transmission line.

Keywords: Overvoltage, lightning, modeling, simulation, overhead transmission line, insulator, surge arrester, grounding, parametric analysis, EMTP.

INTRODUCTION

An overhead transmission line model for lightning overvoltage calculations must include those parts of the line that get involved in its behavior when a lightning return stroke hits a wire (a shield wire or a phase conductor) or a tower, and have some influence on the voltages developed across insulator strings. An adequate representation of a power apparatus or component in transients analysis must be based on the frequency range of the transients to be analyzed [1]. Transients caused by lightning discharges are classified as fast front transients, so the representation

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of an overhead transmission line in lightning overvoltage calculations must be made accordingly.

Overhead transmission lines are usually shielded to avoid a direct impact of lightning strokes to phase conductors, although the surge arrester protection of unshielded lines is presently envisaged as a firm solution for those lines in which a low grounding impedance is difficult to achieve.

After a return stroke hits a tower or a shield wire, the current flows through the shield wire, the tower and the footing resistance; voltages are induced on phase conductors and fast front voltages are superimposed to power frequency voltages across insulator string terminals. If the return stroke hits a phase conductor, the lightning current and voltage surges will flow through the conductor in two directions from the point of impact, being in this case the influence of the tower grounding negligible. When the return stroke hits a phase conductor the overvoltage caused across insulator strings is much greater than the overvoltage that the same stroke would cause if the point of impact was a tower or a shield wire. This is the reason why a good lightning shielding is of paramount importance in the design of overhead transmission lines [2].

The overall phenomenon is very complex, mainly when the return stroke hits a tower or a shield wire, and the development of an accurate model can be a difficult task. A trade off will always exists between the accuracy and the applicability of the model. Simplified models can produce conservative results, which introduce some safety margin.

Surge arresters are usually installed to improve the lightning performance of transmission lines [2]. In general, they are a solution for lines with a poor shielding or for those line sections in which it is very difficult to obtain low enough footing impedances. When arresters are installed, the discharged energy becomes a variable of concern, since it can be the cause of arrester failure.

A very accurate and sophisticated line model is rarely used; in addition, modeling guidelines can be different when the goal is to estimate overvoltages or to determine arrester energy stresses. This paper is aimed at presenting the studies that can be used to select an adequate model for each line component. Next section summarizes the guidelines proposed in the literature for representing transmission lines in lightning studies and the lightning flash characteristics [3]. Section of the Parametric Study is the main core of this paper and presents several studies that will illustrate how to select the representation of each line component as a function of the study goal. The calculation of the lightning flashover rate must be made taking into account the random nature of lightning and the random behavior of some line components; e.g., insulation strength. A Monte Carlo based method can be used for that purpose [3]; the main features of the approach applied in this paper are summarized [3-4].

MODELING GUIDELINES FOR LIGHTNING OVERVOLTAGE CALCULATIONS

Modeling guidelines for representation of overhead transmission lines in lightning overvoltage simulations have been proposed in many references [1, 5-7]. These guidelines, irrespectively of the study goal, can be summarized as follows (see Figure 1):

1) Shield wires and phase conductors of the transmission line can be modeled by several spans at each side of the point of impact. A rigorous representation of each span should be based on a multi-phase frequency-dependent untransposed distributed-parameter line model [8].

   However, for lightning overvoltage calculations, a constant-parameter line model can be accurate enough, and parameters are usually calculated at 400-500 kHz [5]. A line termination at each side of this model is needed to avoid reflections that could affect the simulated overvoltages around the point of impact. This termination must be represented accordingly to the model chosen for the line spans; for instance, if the line spans are represented by line sections with constant and distributed parameters calculated at 500 kHz, the line termination could by a long enough section, whose parameters are also calculated at 500 kHz.
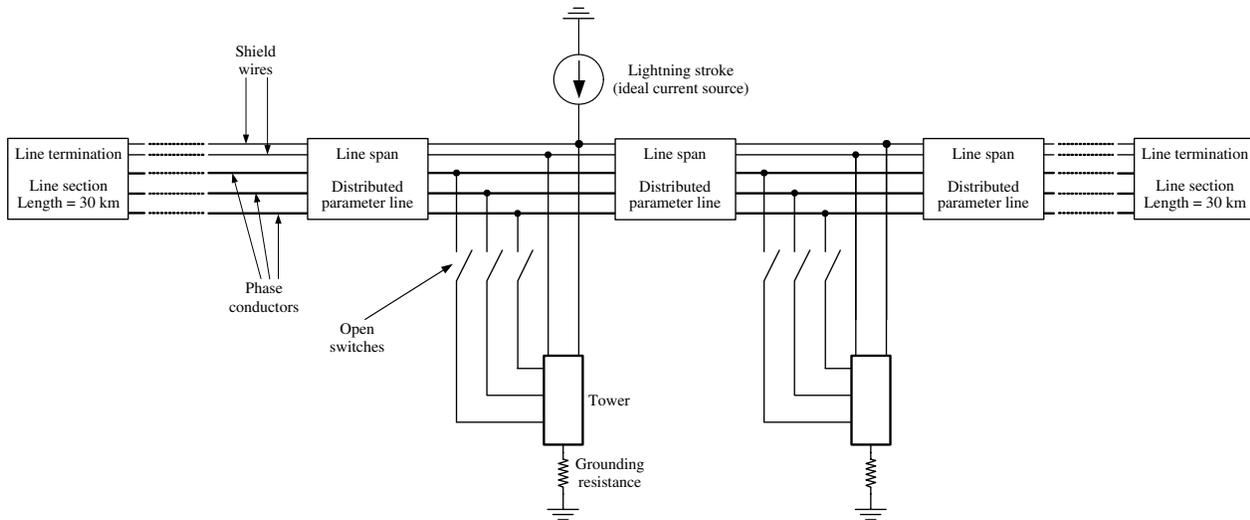
Figure 1. Overhead line model for calculation of lightning overvoltages.

2) Several models have been proposed to represent transmission line towers (single-phase vertical lossless line model, multiconductor vertical line model, multistory model); they have been developed using a theoretical approach or based on an experimental work [9-20]. The simplest representation is a lossless distributed-parameter transmission line, characterized by a surge impedance and a travel time. This model can suffice for lines with towers shorter than 30 m [1]. See [21] for a discussion on tower models.

3) Approaches developed for representation of insulators are based on a voltage-dependent flashover switch, on a voltage-time characteristic, on an integration method or on a physical model [22], which considers the different phases and their dependence on the applied voltage and compute the time to breakdown as the time that is necessary for completion of all the phases of the discharge process [23, 24].

A physical model based on the leader progression model (LPM) can be used to account for non-standard lightning voltages. According to this model, the flashover mechanism consists of three steps: corona inception, streamer propagation and leader propagation. When the applied voltage exceeds the corona inception voltage, streamers propagate along the insulator string; if the voltage remains high enough, these streamers will become a leader channel. A flashover occurs when the leader crosses the gap between the cross-arm and the conductor. Therefore, the total time (t_t) to flashover can be expressed as follows:

$$t_t = t_c + t_s + t_l \tag{1}$$

where t_c is the corona inception time, t_s is the streamer propagation time and t_l is the leader propagation time. Usually t_c is neglected because it is very short in comparison to the other two times. According to [24], t_s can be calculated as follows:

$$t_s = \frac{E_{50}}{1.25E - 0.95E_{50}} \tag{2}$$

where E_{50} is the average gradient at the critical flashover voltage and E is the maximum gradient in the gap before breakdown. The leader propagation time, t_l, can be obtained from the following equation:

$$\frac{dl}{dt} = k_l V(t) \left[\frac{V(t)}{g - l} - E_{l0} \right] \tag{3}$$

where $V(t)$ is the voltage across the gap, g is the gap length, l is the leader length, E_{l0} is the critical leader inception gradient, and k_l is a leader coefficient. The leader propagation stops if the gradient in the unbridged part of the gap falls below E_{l0}.

4) Grounding modeling is a critical aspect. A nonlinear frequency-dependent representation is required to obtain an accurate simulation [25, 26]. Since the information needed to derive such a model is not always available, a lumped circuit model is usually chosen for representing the footing impedance, although it is recognized that this model is not always adequate.

A grounding design based on one or several vertically driven rods has to include soil ionization effect [27, 28]. In such case the grounding model may be represented

by means of a nonlinear resistance whose value is approximated as follows [2, 29, 30]:

$$R_T = \frac{R_o}{\sqrt{1 + I / I_g}} \qquad (4)$$

where R_o is the footing resistance at low current and low frequency, I is the stroke current through the resistance, and I_g is the limiting current to initiate sufficient soil ionization, which is given by:

$$I_g = \frac{E_0 \rho}{2\pi R_o^2} \qquad (5)$$

being ρ the soil resistivity (ohm-m) and E_0 the soil ionization gradient (about 400 kV/m, [28]).

5) Phase voltages at the instant at which the lightning stroke impacts the line have to be included in calculations. For statistical calculations, they are deduced by randomly determining the phase voltage reference angle and considering a uniform distribution between 0° and 360°.

6) A surge arrester model adequate for fast front transients simulation has to show a nonlinear and frequency-dependent behavior. Several models have been developed to reproduce the performance of a MO surge arrester in high-frequency transients [31-37]. The arrester model has to include the length of arrester leads since its effect cannot be always neglected. In this work the arrester model used in calculations is that recommended by IEEE [34].

7) A lightning stroke is represented as an ideal current source (infinite parallel impedance) whose parameters, as well as its polarity and multiplicity, are randomly determined according to the distribution density functions recommended in the literature [2, 38, 39]. A return stroke waveform is defined by the peak current magnitude, I_{100}, the rise time, $t_f (= 1.67 (t_{90}-t_{30}))$ and the tail time, t_h (i.e. the time interval between the start of the wave and the 50% of peak current on tail), see Figure 2.

The statistical variation of the lightning stroke parameters can be approximated by a log-normal distribution, with the following probability density function [39]:

$$p(x) = \frac{1}{\sqrt{2\pi} x \sigma_{\ln x}} \exp\left[-\frac{1}{2}\left(\frac{\ln x - \ln x_m}{\sigma_{\ln x}}\right)^2\right] \qquad (6)$$

where $\sigma_{\ln x}$ is the standard deviation of $\ln x$, and x_m is the median value of x. If two parameters x and y are independently distributed, then $p(x, y)=p(x)p(y)$.

In this work return stroke currents are represented by means of the Heidler model [40]. A conversion procedure has to be performed to derive the parameters of the Heidler waveform from these parameters [41]. See also reference [3] for more details on lightning stroke characteristics and on the Heidler model.
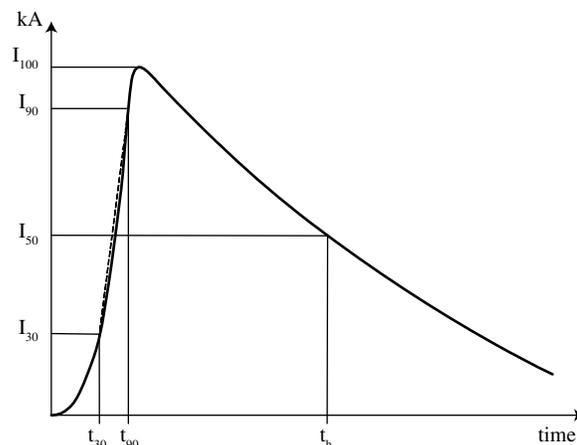

Figure 2. Parameters of a return stroke.

TEST LINE

Figure 3 shows the tower design for the line tested in this paper. It is a 400 kV line, with two conductors per phase and two shield wires, whose characteristics are provided in Table 1.
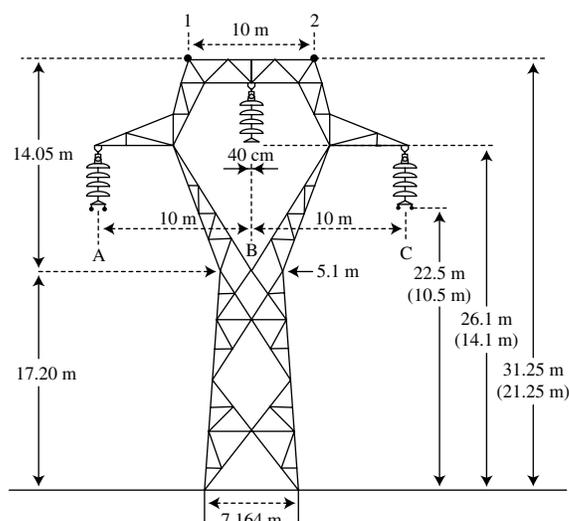

Figure 3. 400 kV line configuration (Values within parenthesis are midspan heights).

Table 1.   Line conductor characteristics.

	Type	Diameter (mm)	Resistance (Ω/km)
Phase conductors	CURLEW	31.63	0.05501
Shield wires	94S	12.60	0.642

Arrester parameters used in this work, and needed to develop the model recommended by IEEE [34], are: height, $d = 3.7$ m; discharge voltage for a 10 kA, 8/20 µs current, $V_{10} = 843$ kV; switching surge discharge voltage for a 1 kA, 30/70 µs current $V_{ss} = 719$ kV.

MONTE CARLO PROCEDURE

The main aspects of the Monte Carlo method used in this study were detailed in [3]. A short summary is presented in the following paragraphs:

1) The calculation of random values includes the parameters of the lightning stroke (peak current, rise time, tail time, and location of the vertical leader channel), phase conductor voltages, the footing resistance and the insulator strength.

2) The last step of a return stroke is determined by means of the electrogeometric model. See reference [2] for a review of electrogeometric models.

3) Overvoltage calculations are performed once the point of impact has been determined.

4) If a flashover occurs in an insulator string, the run is stopped and the flashover rate updated.

5) The convergence of the Monte Carlo method is checked by comparing the probability density function of all random variables to their theoretical functions; the procedure is stopped when they match within the specified error.

PARAMETRIC STUDIES

The development of an overhead transmission line model adequate for lightning studies must be based on two main aspects: what parts of the line must be represented and what model should be selected for each part. Since it is well known what components of the line have to be included in the model, the goal of this section is to justify the representation to be used for each part.

Corona is a physical phenomenon closely related to overvoltages in overhead lines whose influence in surge propagation is not negligible [2]. There is, however, an important drawback when this effect has to be included in line models: most current versions of transients simulation tools do not have corona as a built-in capability. Since simulations without corona will always produce conservative results, this effect is often neglected, given the difficulties to implement it. A discussion about the influence that this omission can have on the ultimate results is included at the end of this section.

Air clearances are not usually included in transmission lines models, since it is assumed that flashovers will always occur across insulator strings. In practical applications, the critical flashover voltage of an air gap for lightning impulse is lower with insulators than without insulators. However, it could be important to consider this possibility in some lines or during the design of the line. The modeling approaches to be used in such cases are the same that were detailed above for insulator strings [2, 22].

The following subsections present the methodology followed in this work for building a line model adequate for calculation of lightning overvoltages and arrester energy stresses.

### Phase conductors and shield wires

Line span models, which include shield wires and phase conductors, can be represented by either a constant-parameter or a frequency-dependent parameter model. When the goal is to calculate overvoltages across insulators or to obtain the flashover rate, a constant-parameter model will generally suffice since the main concern is the effect of the stroke wave front. However, when the goal is to estimate the energy discharged by arresters a constant-parameter model will be a wrong representation. Figure 4 shows the results derived with the test line and two different model approaches; the a) plot shows overvoltages obtained without arresters, the b) plot shows the energy discharged by arresters. According to these results, the peak voltage across insulators obtained with both models is very similar, but the energy values are very different. Note that the voltage wave slope is rather constant during the front of the wave, but it varies during the tail. A constant-parameter model (with parameters calculated at 500 kHz) introduces too much damping during the tail, see the lower plot, as a consequence a significant percentage of the stroke energy is dissipated by wires.

When arresters are installed in towers adjacent to the struck tower, the energies through arresters at this tower increases.

This phenomenon is well known: currents through arresters at adjacent towers are of opposite polarity to the currents through arresters at the struck tower, they flow back to the point of impact, and result in an increase of energy [2].
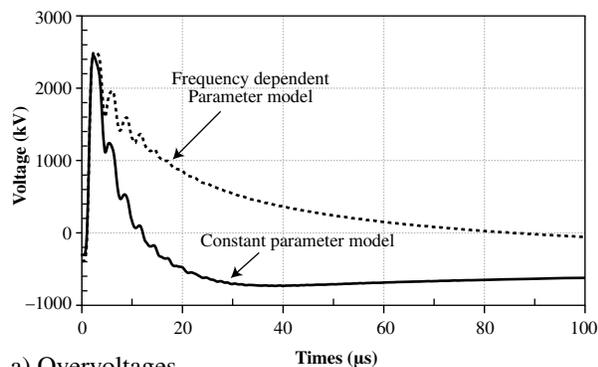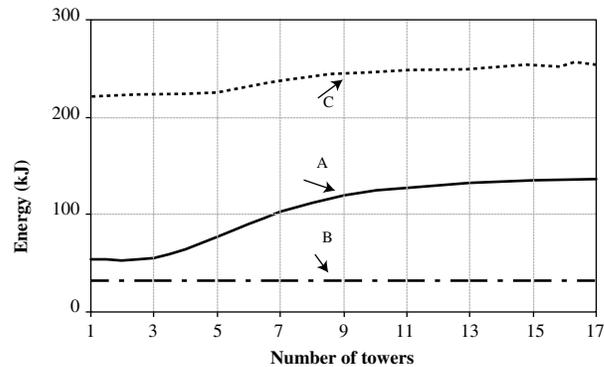
a) Overvoltages
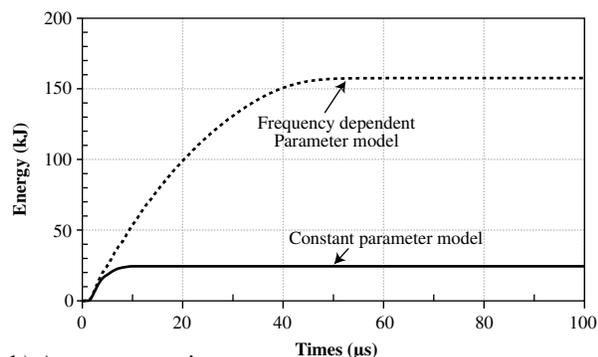
b) Arrester energies

Figure 4.   Influence of the line model. Stroke to a tower. (I_{100} = 150 kA, t_f = 2 μs, t_h = 100 μs, R_o = 400 Ω, ρ = 2000 Ω.m).

a) Stroke to a tower

b) Stroke to a phase conductor

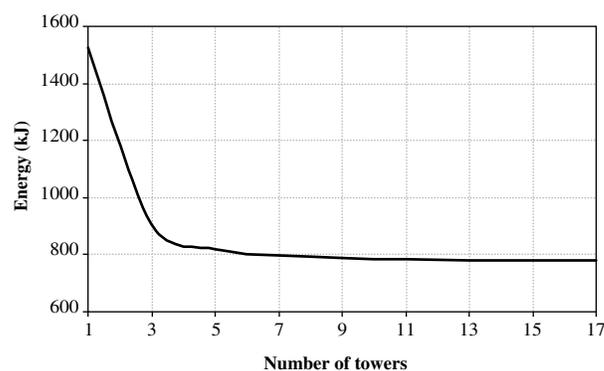Figure 5.   Line arrester energies vs. number of towers with arresters (R_o = 200 Ω, ρ = 1000 Ω.m).

Figure 5 shows the energy discharged by arresters at the three phases (A,B, C) of the struck tower as a function of the number of spans and towers included in the model [42]. The difference between the energy discharged by the three phases is mainly due to the angle of the phases at the instant of impact, see [42]. This result is very important and must be taken into account when developing the line model; otherwise, energy stress calculations would not be accurate enough. For the test line, no less than 7 towers/ spans at each side of the struck tower must be incorporated into the model. Remember, on the other hand, that these results were derived without including corona effect in the line model.

Insulators
Approaches generally used for representing insulator strings are those mentioned in Section Modeling Guidelines. From a physical point of view, the leader progression model is a more realistic approach of an insulator string behavior. However, using adequate parameters for each model, lightning flashover rate could be very similar with all models. The study presented below was aimed at comparing the results derived from two different models using the parameters proposed in the literature.

The models and parameters used in calculations were as follows:

a) A controlled-switch whose strength was calculated according to the expression proposed by IEC 60071-2 for negative polarity strokes and lines located at sea level [29], CFO^- = 700* d_s, where d_s is the striking distance of the insulator string. Since the insulator striking distance is d_s = 3.212 m, a Weibull distribution with CFO^- = 2248 kV, and σ/CFO = 5% was used in calculations.

b) The parameters specified in the leader progression model were k_l = 1.3E-6 m^2/(V^{2}s) and E_{l0} = 570 (kV/m) [24]. The value of the average gradient at the critical flashover voltage, E_{50}, was assumed to be the same that E_{l0}. A Weibull distribution with a standard deviation of 5% was assumed for parameter E_{l0}.

The calculations were performed by:
• Assuming that footing impedances behave as nonlinear resistances with a normal distribution, being the mean resistance value at low current and low frequency 50 Ω and the standard deviation 5 Ω. The soil resistivity was in all studies 500 Ω.m.

- Using a lossless line model for representing towers, whose surge impedance value was calculated according to the modified version of the "waist" model [43].

- Assuming that the median value of the tail time was 77.5 μs, while the values of the standard deviations were [41]: peak current magnitude = 0.740 kA; rise time = 0.494 μs; tail time = 0.577 μs.

Figure 6 shows the flashover rates as a function of the median values of both the peak current magnitude and the rise time of the return stroke current. The conclusions from these results are very obvious: the trend is the same with both models but the differences between the flashover rates obtained with both approaches can be important and they increase with the peak current magnitude and decrease with the rise time. Since the values used to represent both insulator models are those recommended in the literature, one can assume that the leader progression model will provide smaller rates. However, different values from those used in this paper have also been proposed, see for instance [2].

It is important to keep in mind that insulator parameters must be specified taking into account atmospheric conditions [2]. Parameters used in this work are assumed to be measured at standard atmospheric conditions.
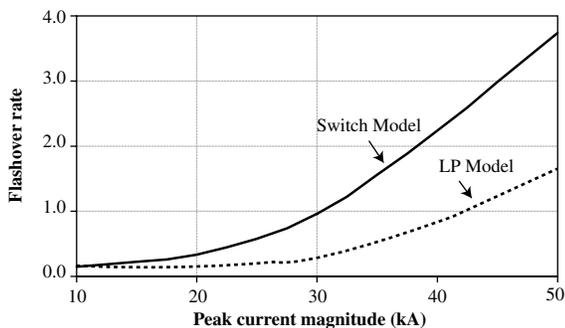
a) Flashover rate vs. peak current magnitude
   (t_f = 2μs, t_h = 77.5 μs)
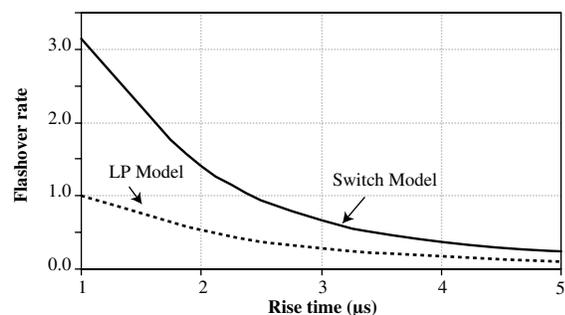
b) Flashover rate vs. rise time
   (I_{100} = 34 kA, t_h = 77.5 μs)

Figure 6. Influence of the insulator string model. (R_o = 50 Ω, ρ = 500 Ω.m, N_g = 1 fl/km²).
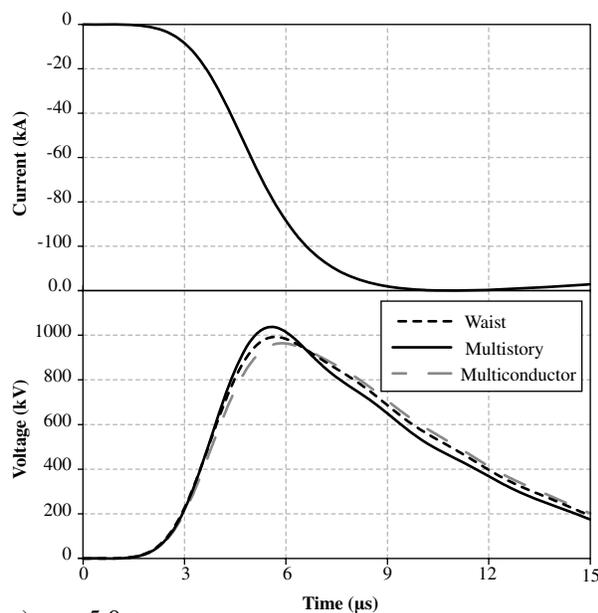
Towers
A study was performed to analyze overvoltages obtained with each tower model. The simulations were made without including insulator strings, which were represented as open switches. Figure 7 shows the overvoltages caused by two different return strokes across the insulator strings of the outer phase. One can observe that the calculated overvoltages are very different with a steep rise time, being much smaller the differences derived with a slow fronted waveform. Flashover rates obtained with each tower model will show differences that can be predicted from the results depicted in Figure 6. The trend is the same with all tower models –the flashover rate increases when the median peak current magnitude increases or the rise time decreases–, but the rate values are different for each model. Only when the median values of the peak current magnitude and the rise time are respectively below 20 kA and above 3 μs, the differences between rates obtained with different models are not very significant [21].

Footing impedance
An accurate model has to account for a decrease of the resistance value as the discharge current value increases [27, 28], and include a frequency-dependent behaviour. Although a significant effort has been made during the last years on the development of more accurate grounding models, very rarely a frequency-dependent model has been used to estimate the lightning behaviour of transmission lines.

However, models based on both a constant resistance and a nonlinear resistance have been frequently applied. Since the resistance value due to soil ionization decreases as the discharge current increases, it is easy to predict what differences are obtained when comparing results derived from the two approaches: higher overvoltage values and higher arrester energy values are obtained with a constant resistance value. The nonlinear resistance model is a more accurate approach and it is recommended in some standards [29, 30]. However, a constant resistance is also recommended [44]; the results derived from its application are then more conservative.

Figure 8 shows the results obtained from a parametric study aimed at analyzing the energy discharged by arresters when they are installed at all phases in all towers of the test line and the lightning stroke hits a tower. The trend of these results is the expected one with the constant resistance model. However, it is interesting to note that with a nonlinear resistance model, the energy discharged by arresters remain constant above a certain value of R_o, although it is very sensitive with respect the soil resistivity. The effect on the resistance model when the stroke hits a phase conductor is less important and negligible for lines with a good shielding.

a) $t_f = 5.0$ μs
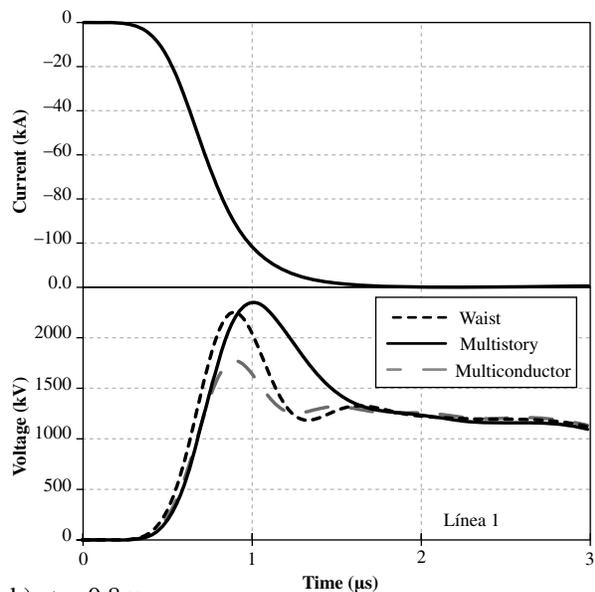
b) $t_f = 0.8$ μs

Figure 7. Tower model performance. ($I_{100} = 120$ kA, $t_h = 77.5$ μs, $R_o = 50$ Ω, ρ = 500 Ω.m).
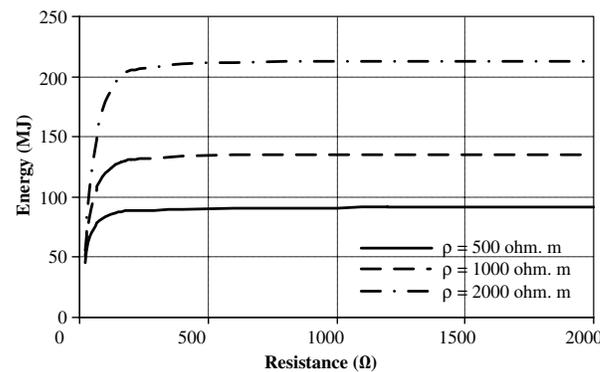
Corona

The air ionization produced around a line conductor when the conductor voltage reaches a critical value implies storage and movement of charges, which can be viewed as an increase of the conductor radius and consequently of the capacitance to ground [2]. The increase in capacitance results in both a decrease in the velocity of propagation and a decrease in the surge impedance. The decrease in

velocity distorts the surge voltage during propagation: the wave front is pushed back and the steepness of the surge is decreased. In general, the crest voltage is also decreased. This effect is illustrated with the example shown in Figure 9.
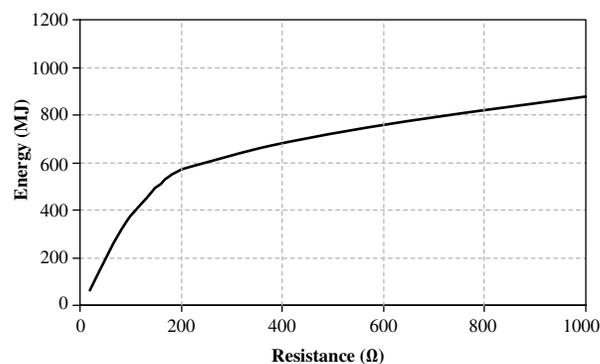
a) Constant resistance

b) Nonlinear resistance

Figure 8. Sensitivity study: Energy discharged by arresters.

The most common corona models are based on a macroscopic description, namely on the so-called charge-voltage curves (*q-v* curves) [2]. Several practical corona models have been developed to date; they are based on a piecewise linear, a parabolic, or a polynomial approach of the *q-v* curves, or represent the corona capacitance as a function of both the voltage and its derivatives with respect to time. See references [45-53].

It is evident that corona effect distorts and reduces the peak voltage of the lightning voltage surge. The results shown in the figure were derived from a single-phase line model without including frequency-dependence of line parameters. As a rule of thumb one can assume that for the length of the line conductors that is usually represented in lightning studies, corona is predominant over the effect of the frequency on the electrical parameters.

An important conclusion from these results is, as mentioned above, that neglecting corona will provide conservative results, so the safety margin to be used in insulation coordination studies can be ever reduced if simulation results were deduced without corona effect in the overhead transmission line model [29-30, 54].
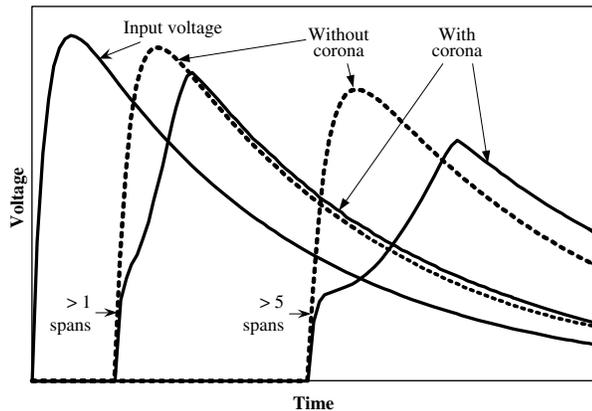

Figure 9.   Voltage distortion during propagation caused by corona.

Other features
- The power frequency voltage peak is more than 30% of the residual voltage of arresters installed at the test line; therefore, one can expect some influence on the energy discharged by arresters. As shown in [42], this energy through the inner phase arrester reaches much lower values than through the outer phase arresters, and there is a dependency between energy stress and phase voltage angle, see Figure 5a. However, only strokes to phase conductors can represent a threat for arresters.
- Arrester leads are usually represented as constant inductances with 1 µH/m. If leads are included in the model,
  - the energies discharged by arresters are different for the three phases when the stroke hits a tower or a shield wire due to differences between phase angles [42];
  - irrespectively of the point of impact, arrester energies show a small dependency with respect the rise time of the return stroke and differences between energy values obtained with and without leads are negligible.

In any case, arrester leads have to be included in the line model because their influence on the voltage across insulator strings is not always negligible.

CONCLUSIONS

Models to be used to determine arrester energy stresses must have some differences with respect the models to be developed for flashover rate calculations.

- Models for arrester energy evaluation have to incorporate more spans than models required for flashover rate calculations. A frequency-dependent model is required when the goal is to estimate arrester energies, although a constant parameter model will suffice for flashover rate calculations.
- The model selected for representing towers from the various approaches developed to date can have some influence on both flashover rates and arrester energy stresses.
- The representation of footing impedances is a critical aspect for calculation of overvoltages and arrester energy stresses caused by strokes to a shield wire or a tower. Differences obtained with different modeling approaches (constant vs. nonlinear and variable) can be very significant.

Table 2 presents a summary of the main conclusions of this study and the recommended guidelines.

Either for flashover rate calculations or for arrester energy studies, a frequency-dependent parameter model is the most accurate representation of line wires, but for flashover rate calculations a representation based on a constant-parameter model will usually suffice.

Although the above models are realistic approaches for simulation of lightning effects, they have some limitations that are worth mentioning. For instance, corona effect was not included in the line span models, voltages induced by the electric and magnetic fields of lightning channels to shield wires and phase conductors were neglected, and footing impedance models were too simple.

Return stroke parameters play an important role in these studies; only single-stroke negative polarity flashes were assumed in this work; more accurate results would have been obtained by assuming that a percentage of return strokes are of positive polarity or including the effect of subsequent strokes. Correlation between stroke parameters is another aspect to be considered.

Table 2.   Modeling guidelines for lightning studies.

Line component	Flashover rate calculation	Arrester energy calculation
Wires	The line can be represented by 3 or 4 untransposed constant distributed-parameter spans at each side of the point of impact. A line termination should be added at each side	The line is represented by 7 or more untransposed frequency-dependent distributed-parameter spans at each side of the point of impact. A line termination should be added at each side.
Towers	The selection can be based on the tower height: a simplified single-phase lossless line model can suffice for towers shorter than 30 m. Above that height a more sophisticated model (multiconductor, multistory) should be used. In any case the model should be carefully selected as significant differences between results derived with each model can be obtained in any type of calculation.	
Insulators	The LPM is a realistic representation of an insulator, although parameters have to be selected very carefully and taking into account atmospheric conditions. Other models can be used, but some experience is advisable to select parameters. Values recommended in standards will usually produce conservative flashover rates.	In general, insulator models do not have to be included in the line model when arresters are installed at all phases, unless arrester leads are too long.
Grounding	Although grounding models should present a nonlinear and frequency-dependent behavior, most works to date are based on either a constant or a nonlinear resistance. Simulation results obtained with these models can be very different from each other. The constant resistance model is used to obtain conservative results. The influence of tower grounding is almost negligible when the stroke hits a phase conductor.	
Arresters	——	Several arrester models have been developed. Similar accuracy can be obtained with most of them. Arrester leads have to be included in the line model because their influence on the insulator voltages can be important.
Boundary conditions	Although they do not have to be neglected, power frequency voltages have a limited influence on overvoltages and flashover rates.	The influence of power frequency voltages is more evident when the stroke hits a tower, but the energy discharged in those cases is rather low and very rarely will exceed the maximum absorption capability of arresters installed in a shielded transmission line.

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