AN EMPIRICAL MODEL FOR ADSORPTION THERMODYNAMICS OF COPPER (II) FROM SOLUTIONS ONTO ILLITE CLAY–BATCH PROCESS DESIGN

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ABSTRACT

The copper causes important health problems risk when it exists at high concentrations in drinking waters and daily feeds. Therefore, in this study, copper adsorption from solutions onto illite clay was investigated in batch mode as a function of the initial solution pH (3-6), temperature (30-60 °C) and ionic strength (0-0.1 mol/L NaCl). The equilibrium was attained within 24 hours. Optimum conditions were determined as pH 6, temperature 60 °C and 0 mol/L NaCl concentration. The isotherm data followed the S-class isotherm. The reason of this S-class isotherm was either solute–solute attractive forces at the surface causing cooperative adsorption or a competing reaction such as complexation with a ligand. Mathematically, the isotherm data were explained with the sum of several single Freundlich models. Also, the thermodynamic parameters of the process were calculated. Positive values of Gibbs free energy change (ΔG°) indicated that the adsorption process was spontaneous. As the enthalpy change (ΔH°) had positive value for all the parameter intervals, copper adsorption was concluded to be physical and endothermic process. The positive entropy values indicated that the randomness at solid-liquid interface increased with concentration decrease. Maximum copper adsorption capacity of illite clay was calculated at 60 °C as 1.823×10⁻⁶ mol/g. Furthermore, an empirical model was developed to determine the thermodynamic parameters of the process and operation conditions of the batch reactor as follows.

Keywords: Copper, illite, S-shaped isotherm, thermodynamics, empirical model

1. INTRODUCTION

The copper is most commonly present in the earth’s crust as chalcopyrite (CuFeS₂), bornite (CuSFeS₃) and chalcocite (Cu₃S). The metallic copper and copper compounds are widely used in many industries such as the petroleum, copper brass, copper ammonium rayon, battery, fertilizer, dye and pigment. Copper is non-biodegradable and persistently accumulates in the food chain and therefore its removal from wastewaters is necessary. As the soil components such as clays and organic acids bond the copper strongly, it is difficult to wash out the copper from contaminated soils. Copper is a toxic and mutagenic element for humans and causes brain, skin, pancreas and heart diseases. Copper limit value for drinking water and wastewater discharge is proposed as 1.3 mg/L. Also, maximum copper concentration for irrigation purposes is interfered two tetrahedral silica layers. Two unit illite layers are bounded to each other by potassium cations. The potassium cations hinder the water chain and therefore its removal from wastewaters is necessary. Copper compounds are widely used in many industries such as the petroleum, copper brass, copper ammonium rayon, battery, fertilizer, dye and pigment.

The obtained results from the adsorbent investigations in the last two decades have made the adsorption technology one of the cost-effective methods for wastewater treatment. Although the activated carbon is one of the most effective adsorbents against heavy metals, it requires chelating agents to enhance its performance, and therefore its use is expensive. The metallic copper and copper compounds are widely used in many industries such as the petroleum, copper brass, copper ammonium rayon, battery, fertilizer, dye and pigment. Copper is non-biodegradable and persistently accumulates in the food chain and therefore its removal from wastewaters is necessary. As the soil components such as clays and organic acids bond the copper strongly, it is difficult to wash out the copper from contaminated soils. Copper is a toxic and mutagenic element for humans and causes brain, skin, pancreas and heart diseases. Copper limit value for drinking water and wastewater discharge is proposed as 1.3 mg/L. Also, maximum copper concentration for irrigation purposes is interfered two tetrahedral silica layers. Two unit illite layers are bounded to each other by potassium cations. The potassium cations hinder the water chain and therefore its removal from wastewaters is necessary. Copper compounds are widely used in many industries such as the petroleum, copper brass, copper ammonium rayon, battery, fertilizer, dye and pigment.

2. EXPERIMENTAL PROCEDURE

2.1 Illite Clay

The used illite sample was collected from a deposit in Ünye-Ordu in Turkey. The X-Ray Diffraction (XRD) pattern of the illite sample was given in Figure 1. The chemical analysis results of illite sample were as follows: SiO₂ (45.67%), Al₂O₃ (36.88%), K₂O (8.9%), MnO (0.82%), F (0.64%), Na₂O (0.31%), H₂O (6.78%). Illite sample was dried at 103 °C during 24 hours in a furnace and sieved to 45–90 μm particle size fractions before being used. The structural block of the illite was given in Figure 2.

2.2 Adsorption Studies

The experimental parameters and their intervals were given in Table 1. All the studied solution concentrations were prepared from the stock solution having a copper concentration of 1.5738×10⁻⁵ mol/L. Copper solutions were prepared using copper chloride, CuCl₂·2H₂O. An automatic pipette was used for concentration adjustment. The solid-to-solution ratio for each experiment was 0.25 g/50 mL. Solution pH levels were adjusted by appropriate droplets of diluted acid (HCl) and base solutions (NaOH). A pH meter was used for pH measurements (WTW, Germany). The ionic strength of the solutions was adjusted with appropriate volumes of 1 mol/L NaCl solution. The experiments
were carried out in batch mode using a temperature controlled incubator shaker (ZHICHENCG, China). The experimental procedure was as follows: Firstly, a desired concentration of copper solution was prepared as 50 mL and the pH of the solution was adjusted and the weighted amount of illite was added to the solution and finally the prepared solution was reacted in a temperature controlled incubator shaker. After reaction, 10 mL solutions were centrifuged at 10,000 rpm during 5 min and 5 mL solutions taken for dilutions. The diluted copper solutions were analyzed at 324.7 nm using an atomic absorption spectrometer (AAS) (UNICAM, England). The samples were automatically measured three times in one aspiration by the AAS. The relative standard deviation (RSD) for the used AAS was generally in the range of 0 - 3%. The flame type of the AAS was air-acetylene. Standard solutions prepared for calibration curve had a concentration range of 0-10 mg/L. A mass balance equation was used to calculate the adsorption capacity of illite as follows.

\[
Q_e = \left((C_0 - C_e) \times \frac{V}{W}\right)
\]

Where, \(C_0\) and \(C_e\) are the solution copper concentrations at initial and equilibrium (mol/L), \(Q_e\) is the adsorption capacity at equilibrium (mol/g), \(V\) is the solution volume (L), \(W\) is the mass of illite added to the solutions (g).

Table 1: The intervals of experimental parameters.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>3, 4, 5.14, 6</td>
</tr>
<tr>
<td>Temperature, ºC</td>
<td>30, 40, 50, 60</td>
</tr>
<tr>
<td>Ionic Strength, M</td>
<td>0, 0.001, 0.01, 0.10</td>
</tr>
<tr>
<td>Concentration, M</td>
<td>1.574-18.884×10(^{-4})</td>
</tr>
<tr>
<td>Solid-to-solution ratio, g/50 mL</td>
<td>0.25</td>
</tr>
<tr>
<td>Agitation Speed, rpm</td>
<td>150 rpm</td>
</tr>
<tr>
<td>Equilibrium Time, h</td>
<td>24</td>
</tr>
</tbody>
</table>

3. RESULTS AND DISCUSSION

In this study, copper adsorption onto illite clay was investigated as a function of solution pH, temperature and ionic strength. Furthermore, an empirical model that enables to calculate the thermodynamic parameters and operation conditions of the batch process was developed.

3.1 Effect of Parameters

3.1 Effect of pH

Solution pH level significantly affects cation adsorption onto clays because it determines the surface charge \(^{17}\). Also, ionization degree of the cations is depended on the solution pH level \(^{18, 22}\). The effect of initial pH on copper adsorption onto illite was studied at pH range of 3-6 and other parameters were kept constant. The results were given in Figure 3. When the solution pH was increased from 3 to 6, the capacity of the illite increased from 1.185 to 1.698×10\(^{-5}\) mol/g. This result was attributed to that the surface of the illite mineral became negative at high pHs and thereby the capacity increased. On the other hand, the competitive adsorption occurred between hydrogen ions and copper for fixation sites on illite surface and hence capacity decreased at low pHs \(^{23}\). Similar pH effect was reported for cation adsorption onto illite clay \(^{3, 18}\) and Alvarez-Puebla and coworkers reported that copper adsorption increased with pH increase of solution \(^{20}\). Also, Gu and coworkers reported two distinct mechanisms for metal adsorption onto illite: (i) nonspecific ion-exchange reaction occurring on the \(≡\text{SiO}^-\) and \(≡\text{AlO}^-\) sites at low pH values (3-6) (ii) specific adsorption occurring on the \(≡\text{SiOH}\) and \(≡\text{AlOH}\) sites at high pH (6-9) values \(^{23}\).

![Figure 1: XRD pattern of illite clay](image)

![Figure 2: Block structure of illite mineral](image)

![Figure 3: pH effect on copper adsorption (Concentration: 1.574-18.884×10\(^{-4}\) mol/L, Solid-to-solution ratio: 0.25g/50 mL, Temperature: 30 ºC, ionic strength: 0 mol/L)](image)
Figure 4. As can be seen in Figure 4, the copper adsorption decreased with increasing sodium concentration. This result was due to competitive adsorption of sodium cations against copper. In a study, Gu and coworkers studied the adsorption of Cd(II), Cu(II), Ni(II), Pb(II) and Zn(II) on illite at different ionic strength concentrations (0.001-0.1 mol/L NaNO₃). Similarly, Gu and coworkers reported that adsorbed amount of all the cations increased when the ionic strength was decreased. Özmetin et al. also reported that copper adsorption capacity of illite clay decreased with increasing ionic strength as the competitor sodium cations occupied more binding sites.

![Figure 4: Ionic strength effect on copper adsorption](image)

**Figure 4:** Ionic strength effect on copper adsorption (Concentration: 1.574-18.884x10⁴ mol/L, Solid-to-solution ratio: 0.25g/50 mL, Temperature: 30°C, pH: 5.14 (natural)).

The high temperatures made the copper ions more energetic, which led to an endothermic reaction. At temperatures such as complexation with a ligand, copper ions can react with surface sites through the external liquid film layer surrounding the illite particle. The copper adsorption onto illite was endothermic reaction because the higher temperatures increased the capacity. Similar temperature effect was reported in the adsorption of cationic methyl violet and methylene blue dyes on illite surfaces.

3.3 Effect of Temperature

The results for temperature effect in copper adsorption onto illite were given in Figure 5. As can be seen in Figure 5, when the solution temperature was increased from 30 to 60°C, the capacity of illite increased from 1.476 to 1.823x10⁻³ mol/g. The high temperatures made the copper ions more energetic to react with surface sites. On the other hand, the high temperatures decreased the viscosity of the solution and this resulted in easily diffusion of copper ions through the external liquid film layer surrounding the illite particle. The copper adsorption onto illite was endothermic reaction because the high temperatures increased the capacity.

![Figure 5: Temperature effect on copper adsorption](image)

**Figure 5:** Temperature effect on copper adsorption (Concentration: 1.574-18.884x10⁴ mol/L, Solid-to-solution ratio: 0.25g/50 mL, pH: 5.14 (natural), Temperature: 30, 40, 50, 56°C).

3.4 Adsorption Isotherm for Copper Adsorption

The isotherm data fitted the S-class isotherm reported by Giles and coworkers. The isotherm data given in Figure 3-5 were explained by the sum of several single Freundlich models and the model equation was given in below.

\[ Q_e = X_1C_e^3 + X_2C_e^2 + X_3C_e + X_4C_e^0 \]  

(2)

Where, \( Q_e \) is maximum adsorption capacity at equilibrium (mol/g), \( C_e \) is equilibrium solution concentration (mol/L), \( X_1, X_2, X_3, X_4 \) are equation constants.

The coefficient of determination values for the suggested model (Eq. 2) were given in Table 2. As can be seen in Table 2, the coefficients of determination values have acceptable importance (0.984-0.998).

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Model</th>
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<tr>
<td>Temperature</td>
<td>Ionic strength</td>
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<tr>
<td>40</td>
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</table>

3.5. Developed Empirical Model for Process Thermodynamics

To improve an empirical model that is useful for determination of optimum design parameters of a batch reactor using the Eq. (2), the isotherm data were analyzed with Statistica 7.0 programme. In the analysis of data set 107 items of experimentally obtained data were put into analysis. In the analysis, non-linear estimation section of the programme was used for specific regression analysis. It was thought that the constants \( X_1, X_2, X_3, X_4, X_7, X_9 \) and \( X_6, X_8, X_9 \) represent the effects of parameters such as pH, temperature and ionic strength. Therefore these constants (\( X_1, X_2, X_3, X_4, X_7, X_9 \)) were replaced with \( \text{pH}, \text{temperature} \) and ionic strength in the model. Also, equilibrium solution concentration values (\( C_e \)) in Eq (2) were replaced with the initial concentration term (\( C_i \)) in the model to make the model more useful. The developed empirical model was as follow.

\[ Q_e = 492.148 \times 10^{-9} \times [T]^{2.2525} \times [H^+]^{0.2525} \times [C_i]^{0.4236} + 18.38426 \times [T]^{0.11409} \times [I]^{0.10567} \times [C_i]^{0.22765} - 1.327354 \times 10^{-6} \times [T]^{0.22985} \times [H^+]^{-0.417867} \times [I]^{-0.15983} \times [C_i]^{0.32936} \]  

(3)

Where, \( Q_e \) is the model response for the adsorption capacity (mol/g), \( [H^+] \) is molar concentration of hydrogen ions (mol/L), \( T \) is temperature (K), \( [I] \) is molar concentration of sodium ions in the solution (mol/L), \( C_i \) is initial concentration of copper in the solution (mol/L). The model plot for \( (Qe, experimental) \) versus \( (Qe, predicted) \) was given in Figure 6 and coefficient of determination value of the plot was 0.9823.

Thermodynamic analysis of the adsorption data gives information about the spontaneity and nature of the adsorption process. The Gibbs free energy change is a function of equilibrium constant, enthalpy and entropy as follows.

\[ \Delta G^° = -RT\ln K_d \]  

(4)

\[ \Delta G^° = \Delta H^° - T\Delta S^° \]  

(5)

If two equations given above are combined, we get

\[ \ln K_d = - \frac{\Delta G^°}{RT} = \frac{\Delta S^°}{R} - \frac{\Delta H^°}{RT} \]  

(6)
Where, \( AG^\circ \) is the free energy change (kJ/mol). \( AH^\circ \) is the enthalpy change (kJ/mol). \( AS^\circ \) is the entropy change (kJ/mol K). \( K_0 \) is the equilibrium constant \((L/g)\). \( T \) is absolute temperature (K) and \( R \) is the universal gas constant \((8.314 \text{ J/mol K})\). Thus \( \Delta H^\circ \) and \( \Delta S^\circ \) can be determined from the slope and intercept of the linear Eq. (6) respectively.

\[
K_0 = \frac{Q_e}{C_e} = \frac{\text{model value}}{\text{response value}}
\]

\[
K_c = \frac{Q_e}{C_e} = \frac{\text{model value}}{\text{response value}}
\]

Where, \( K_c \) is the equilibrium constant \((L/g)\). \( Q_e \) is the model value of adsorbent input to the reactor (kg). \( C_0 \) and \( C_e \) are the initial and equilibrium concentrations of copper in the liquid phase (mol/L). \( Q \) is the mass of adsorbent input to the reactor (kg). \( W \) represents the response of the adsorption onto surface and decreased the adsorption-desorption rate. The developed model given in Eq. 3 was also found as useful for calculation of thermodynamic parameters of the process for a given experimental condition by replacing \( K_0 \) value with the response \( Q_e \) and by dividing the model to the \( C_0 \) value. The developed thermodynamic model was given in below.

\[
\begin{align*}
K_0 &= \frac{492.148 \times 10^{-3} \times T^{1.2232} \times [H^+]^{6.157} \times [H^+]^{6.157} \times [C_0]^{0.057} \times 18.38426 \times T^{1.0262} \times [H^+]^{6.157}}{C_e} \\
\end{align*}
\]

\[
\begin{align*}
K_c &= \frac{1.327354 \times 10^{-6} \times T^{1.2232} \times [H^+]^{6.157} \times [H^+]^{6.157} \times [C_0]^{0.057} \times 18.38426 \times T^{1.0262} \times [H^+]^{6.157}}{C_e}
\end{align*}
\]

The results of thermodynamic analysis were given in Table 3. Positive value of enthalpy (\( AH^\circ \)) indicated that the process had endothermic nature. While the enthalpy range for physical adsorption is between \(-20 \) to \(-40 \text{ kJ/mol}\), this value for chemisorption is between \(-400 \) and \(-80 \text{ kJ/mol}\). The enthalpy change values were in the range of 10.327 and 61.790 \text{ kJ/mol}. The positive value of enthalpy indicated that copper adsorption was physical in nature. Although the process was physical in nature, the capacity of the illite increased with temperature increase. This result was attributed to the increasing vibration energy of copper ions to react with illite at high temperatures. In the pH effect section, the mechanism given based on initial pH value was non-specific ion exchange reaction, and therefore in respect to enthalpy value the ion exchange reaction is generally between physical adsorption and chemical sorption. But the mechanism was found as physical adsorption in our study based on thermodynamic investigation. Because \( \Delta H \) values were found in the range of 10.327 and 61.790 \text{ kJ/mol}. We considered that the physical adsorption was dominant in copper adsorption because the isotherm shape of copper adsorption onto illite indicates that solid-solid attractive forces were dominant in copper adsorption indicating physical adsorption. Also, the free energy change (\( AG^\circ \)) had positive value for all the parameter intervals and the process was concluded to be unspontaneous. Adsorption-desorption rate at solid-solution interface decreased due to decreasing entropy change with increasing concentration (Table 3). This result was due to the increasing solute-solute attractive forces which increased the copper adsorption onto surface and decreased the adsorption-desorption rate. The developed model given in Eq. 3 was also found as useful for calculation of thermodynamic parameters of the process for a given experimental condition by replacing \( K_0 \) value with the response \( Q_e \) and by dividing the model to the \( C_0 \) value. The developed thermodynamic model was given in below.

\[
\begin{align*}
V \times (C_0 - C_e) &= Q_e \times W
\end{align*}
\]

\[
\begin{align*}
\text{Figure 7:} \quad \text{The plot for } \Delta G^\circ \text{experimental versus } \Delta G^\circ \text{predicted}
\end{align*}
\]

3.6 Batch Process Design

It is well known that the isotherm models are useful equations to design the single stage batch reactors. For this purpose, the developed empirical model (Eq. 3) was used to design a batch reactor which was illustrated in Figure 8. The mass balance equation for the first stage of design can be given as follows.

\[
W = 492.148 \times 10^{-4} \times T^{1.2232} \times [H^+]^{6.157} \times [H^+]^{6.157} \times [C_0]^{0.057} \times 18.38426 \times T^{1.0262} \times [H^+]^{6.157} \\
\times [C_0]^{0.057} \times [C_e]^{0.057} \times 1.327354 \times 10^{-6} \times T^{1.2232} \times [H^+]^{6.157} \times [H^+]^{6.157} \times [C_0]^{0.057} \times 18.38426 \times T^{1.0262} \times [H^+]^{6.157} \\
\times [C_e]^{0.057}
\]

The plots for required mass of illite against volumes of treated wastewater were given in Figure 9. The selected parameters for model wastewater were as follow: copper concentration \(18.884 \times 10^{-5} \text{ mol/L}\), pH 6, temperature 333.15 K, ionic strength 0.1 M.
Table 3: The values of thermodynamic parameters as function of concentration, temperature, pH and ionic strength.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Concentrations, (mol/L)×10^-5</th>
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<tbody>
<tr>
<td></td>
<td>4.721</td>
</tr>
<tr>
<td></td>
<td>( \Delta H^o )</td>
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<tr>
<td>pH</td>
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<td>5.14</td>
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</tbody>
</table>

Figure 9: The plots for required masses of illite against volumes of treated wastewaters at different removal efficiencies.

4. CONCLUSIONS

In this study, the copper adsorption by illite clay was studied and the main results were as follows:
- The adsorption capacity of the illite increased with pH increase and capacity values for 3, 4, 5.14, 6 pH values were 1.185, 1.288, 1.476, 1.698×10^-5 mol/g respectively.
- The temperature increase raised the capacity and capacity values for 30, 40, 50, 60°C temperature values were 1.476, 1.629, 1.726, 1.823×10^-5 mol/g respectively.
- The ionic strength increase decreased the capacity and, capacity values for 0, 0.001, 0.01, 0.1 M ionic strength values were 1.476, 1.296, 1.143, 0.991×10^-5 mol/g respectively.
- The isotherm data followed the S-class isotherm. It was considered that the reason of this S-class isotherm was either solute-solute attractive forces at the surface causing cooperative adsorption or a competing reaction such as complexation with a ligand.
- The positive enthalpy values changing in the range of 10.327 and 61.790 kJ/mol showed that the process was physical and endothermic in nature. The process was unspontaneous for all the studied parameter intervals. The adsorption desorption rate increased due to positive value of entropy increasing with decreasing concentration.
- The data could be described by the developed model at 99.1% range and the model was useful for design of the batch reactor at tested experimental conditions. Also, the developed model enabled to calculate the thermodynamics of the illite-copper process.
- The selected parameters for model wastewater to design batch process were as follow: copper concentration 18.884×10^-5 mol/L, pH 6, temperature 333.15 K, ionic strength 0.1 M. The analysis results exposed that to treat the above given wastewater having 10 m³ volume, 359.4 kg illite required.
- The results showed that the illite mineral would be used effectively in removal of copper from liquid wastes. The adsorption process in which the illite was used for removal of copper was considered advantageous over ion exchange, reverse osmosis, electrocoagulation, etc. because the illite is a quite cheap adsorbent.

ACKNOWLEDGEMENT

The authors are grateful for financial support of Balıkesir University Scientific Research Project Department (Project No: 2006/30)

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